

**Third Semester FYUGP Degree Examination NOVEMBER
2025**

KU3VACCMT202// - LINEAR PROGRAMMING

2024 Admission onwards

Time : 1.5 hours

Maximum Marks : 50

Section A

Answer any 6 questions. Each carry 2 marks.

1. A maximization assignment problem is transformed into a minimization problem by:
 - (a) subtracting each element of the profit matrix from the highest element of the matrix
 - (b) subtracting all the elements in a column from the highest element of that column
 - (c) subtracting all the elements in a row from the highest element of that row
 - (d) none of the above
2. The minimum number of lines covering all zeroes in a reduced cost matrix of order n can be at least:
 - (a) n
 - (b) $n - 1$
 - (c) $n + 1$
 - (d) at most n (Note: The options provided in the source are mixed. The minimum number of lines is $\leq n$.)
3. Given a system of m simultaneous linear equations in n unknowns ($m < n$), then the number of basic variables will be:
 - (a) m
 - (b) $n - m$
 - (c) $m + n$
 - (d) n
4. Define **surplus variable**.
5. Which of the following is not the characteristics of linear programming
 - (a) Resources must be limited
 - (b) Only one objective function;
 - (c) Parameters value remains constant during the planning period
 - (d) The problem must be of minimization type

6. Define a convex set with an example.
7. What is **degeneracy** in a Transportation problem?
8. The initial solution of a T.P. can be obtained by applying any known method. However, the only condition is that:
 - (a) The solution must be optimum.
 - (b) The solution should be non-degenerate.
 - (c) The $\sum \text{supply} = \sum \text{demand}$ conditions are satisfied.
 - (d) All of the above.

Section B

Answer any 4 questions. Each carry 6 marks.

9. What are the advantages of Linear programming ?
10. What are the components of Linear programming model, Explain briefly.
11. Solve by graphical method. Maximize $Z = 2x_1 + x_2$ subject to

$$\begin{aligned} x_1 + 2x_2 &\leq 10 \\ x_1 + x_2 &\leq 6 \\ x_1 - x_2 &\leq 2 \\ x_1 - 2x_2 &\leq 1 \\ x_1, x_2 &\geq 0 \end{aligned}$$
12. Write the **general mathematical model** of a transportation problem.
13. Find an **initial basic feasible solution** to the following transportation problem using **Matrix-Minima method** (Least Cost Method).

	D_1	D_2	D_3	D_4	Supply
S_1	6	4	1	5	14
S_2	8	9	2	7	16
S_3	10	3	6	2	5
Demand	6	10	15	4	

14. Use **VAM method** (Vogel's Approximation Method) to find an **initial BFS** to the following Transportation problem.

	I	II	III	IV	Supply
A	5	1	3	3	34
B	3	3	5	4	15
C	6	4	4	3	12
D	4	1	4	2	19
Demand	21	25	17	17	80

Warehouses

Section C

Answer any 1 questions. Each carry 14 marks.

15. (a) An advertising company has to assign four projects (P_1, P_2, P_3, P_4) to four designers (D_1, D_2, D_3, D_4). The expected profit (in thousands) is given below. Use the **Hungarian Method** to find the assignment that **maximizes total profit**.

Designers	P_1	P_2	P_3	P_4
D_1	82	83	69	92
D_2	77	37	49	92
D_3	11	69	5	86
D_4	8	9	98	23

- (b) A company has four machines and four jobs to be assigned. The cost of assigning each machine to each job (in rupees) is given in the following table:

Machines / Jobs	Job 1	Job 2	Job 3	Job 4
Machine A	9	2	7	8
Machine B	6	4	3	7
Machine C	5	8	1	8
Machine D	7	6	9	4

Use the **Hungarian Method** to find the optimal assignment that minimizes the total cost. Find the **minimum total cost** of the assignment.

16. Use simplex method to solve the L.P.P.:

$$\begin{aligned}
 &\text{Maximize } z = 2x_1 + 3x_2 \\
 &\text{subject to } x_1 + x_2 \leq 4, \\
 &\quad \quad \quad -x_1 + x_2 \leq 1, \\
 &\quad \quad \quad x_1 + 2x_2 \leq 5, \\
 &\quad \quad \quad x_1, x_2 \geq 0.
 \end{aligned}$$